

# MECHANICAL EVALUATION OF THE HETROJUNCTION LAYERS IN SOLAR PHOTOVOLTAIC CELLS

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### ABSTRACT

Being good candidate materials for solar cell absorbers due to their high absorption and resistance to deterioration, the hetrojunction layers compounds in solar photovoltaic cells CuInSe<sub>2</sub>, CuInS<sub>2</sub>, AgGaSe<sub>2</sub>, and AgGaS<sub>2</sub> are evaluated from the continuum mechanics point of view. Using Orthonormal Decomposition Method (ODM), namely, Orthonormal Tensor Basis Method (OTBM), the tetragonal structure is decomposed into two parts; isotropic (two terms) and anisotropic parts. The overall elastic stiffness is used for comparison among these layers compounds, and for correlation with the calculated bulk modulus and lattice constant. A scale quantitative comparison of the contribution of the anisotropy to the elastic stiffness and to quantify the degree of anisotropy in an anisotropic material is investigated using the Norm Ratio Criteria (NRC). Moreover, the norm and norm ratios are found to be very useful for selecting suitable materials for electro-optic devices, acousto-optic devices and solar photovoltaic cells.

Keywords: Solar Cells, Absorber Layer Compounds, Bulk Modulus, Overall Stiffness.

### **1. INTRODUCTION**

The window layer compounds CuInSe<sub>2</sub>, CuInS<sub>2</sub>, AgGaSe<sub>2</sub>, and AgGaS<sub>2</sub> have a chalcopyrite structure that is closely related those of zinc blend and wurtzite structures. These compounds are found in many applications such as fiberglass communication, thin film solar cells, and photovoltaic systems. Thin film solar cells made from ternary chalcopyrite compounds, such as the aforementioned hetrojunction layers, are characterized by low-cost and clean energy sources. Their high absorption and resistance to deterioration make them good candidate materials for solar cell absorbers. Moreover, due to their flexible optical properties and good stabilities, they are promising compounds for fabricating polycrystalline thin film hetrojunction solar cells [1-3]. Yet, the significant discrepancy in the efficiency of solar cells between the laboratory scale, over 19% [3], and the commercial one, around 13 %, is due to the lack of fundamental understanding of interface and junction properties in the film.



Various attempts have been made to correlate the bulk modulus of compound semiconductors and chalcopyrite compounds with many other physical parameters [4-18]. Nevertheless, it is found that bulk modulus interconnected well with strength and hardness in many materials [5]. Therefore, the material stiffness and its corresponding bulk modulus is one of the important factors that characterize the physical property of a material system which quantifies the degree of stiffness or the energy required to produce a given volume deformation. With a good agreement result, an empirical expression for the bulk modulus was obtained by Cohen [4] based on the nearest-neighbor distance. Using the total energy method Lam et al. [6] obtained an expression for bulk modulus with acceptable results. The bulk modulus for the semiconductor compounds was found to be inverse proportionally correlated to the lattice constants [14, 15]. Gaith et al [16-18] have studied the correlation between the bulk modulus and the over all stiffness and lattice constants for CdX and ZnX (X=S, Se, and Te) using orthonormal decomposition method (ODM) [16] from continuum mechanics point of view. The goal of this study is to understand how qualitative ground state concepts of the hetrojunction layer compounds, CuInSe<sub>2</sub>, CuInS<sub>2</sub>, AgGaSe<sub>2</sub>, and AgGaS<sub>2</sub>, such as overall elastic stiffness, can be related to bulk modulus and lattice constants. Therefore, using the elastic coefficients for anisotropic material, an elastic stiffness scale for such anisotropic material, and a scale to quantify the isotropic elasticity within the material will be discussed.

### 2. THEORY

In comparison of different materials or different geometrical symmetries, or even in a quantitative comparison, for a given material, of the contribution of the anisotropy to a physical property [19-21], the magnitudes of the decomposed parts can give, at certain conditions, valuable information about the origin of the physical property under examination [19, 21]. These problems can be approached by define the norm of a tensor. The norm is invariant and not affected by any transform of the coordinate system. From a device point of view, the new insights facilitate the comparison of materials; one wants to be able to state that a particular material is better than another for making solar cells [20]. The norm concept is very effective for selecting suitable materials for electro-optic devices, transducers, modulators, acousto-optic devices. Based on building up an orthonormal tensor basis elements using the form-invariant expressions [22-26], Gaith et al. [21] developed a decomposition procedure to explore the physical understanding of materials. Hence, following the same procedure, the tetragonal symmetry tensor is decomposed into several independent orthonormal parts. The number of elements of the decomposed stiffness tensor should be equal to the number of nonvanishing distinct stiffness coefficients, i.e., six constants for tetragonal materials, that can completely describe the elastic stiffness in that medium. Thus, using Orthonormal Decomposition Method (ODM), namely, Orthonormal Tensor Basis Method (OTBM) [16, 21], the matrix representation for



the elastic stiffness with tetragonal symmetry system is decomposed into a contracted form as shown in Eq. (1):

where

$$A_{1} = \frac{1}{90} (2C_{11} + 2C_{12} + C_{33} + 4C_{13})$$

$$A_{2} = \frac{1}{45} (2C_{11} - C_{12} + 6C_{44} + 3C_{66} + C_{33} - 2C_{13})$$

$$A_{3} = \frac{1}{90} (-3C_{11} - C_{12} - 4C_{44} - 2C_{66} + 6C_{33} - 2C_{13})$$

$$A_{4} = \frac{1}{144} (-6C_{11} - 10C_{12} + 8C_{44} + 4C_{66} + 16C_{13})$$

$$A_{5} = \frac{1}{16} (-2C_{11} + 2C_{12} + 8C_{44} - 4C_{66})$$

$$A_{6} = \frac{1}{8} (-2C_{11} + 2C_{12} + 4C_{66})$$

(1)

(2)



Where  $A_1$  to  $A_6$  are constants in terms of elastic stiffness coefficients expressed as in Eq. (2). It can be observed clearly that the first two terms on the right hand side are identical to the corresponding well known two terms namely bulk and shear [21] which are identical to those found in literature [27] for the isotropic system [28]. Here,  $A_1$  and  $A_2$  defined in Eq. (2), are the Voigt average polycrystalline bulk *B* and shear modulus *G*, respectively. Hence, it can be stated that the tetragonal system is discriminated into the sum of two parts: isotropic part (first two terms), and anisotropic part (other four terms). The latter part resembles the contribution of the anisotropy on elastic stiffness in the tetragonal system.

Due to the fact that the norm is invariant for the material, it was used for a Cartesian tensor as a parameter representing and comparing the overall stiffness of anisotropic materials of the same or different symmetry or the same material with different phases [16, 19-21]. The larger the norm value is, the more the elastic stiffness of the material is. The concept of the modulus of a vector, norm of a Cartesian tensor is defined as [21]:

$$N = \|C\| = \left\{ C_{ij} \, \mathbf{g} C_{ij} \right\}^{\frac{1}{2}} \tag{3}$$

#### 3. RESULTS AND DISCUSSION

In solar energy technology, thin film solar technology based on the hetrojunction layer compounds CuInSe<sub>2</sub>, CuInS<sub>2</sub>, AgGaSe<sub>2</sub>, and AgGaS<sub>2</sub>, is very promising due to lower production costs and shorter energy pay back times [29]. For these compounds, the successful interface between absorber and buffer layers with alternative materials requires structural and optical material characterization as a prerequisite for understanding interfaces in photovoltaic devices [29]. On the other hand, stability of these compounds in solar cells is of concern due to their application in space, where the cells have to withstand high energy particles, mainly electrons and protons that can cause severe damage in solar cells up to a complete failure. Therefore, the radiation hardness and damage mechanism of the hetrojunction layer compounds solar cells is associated with the overall elastic stiffness and bulk modulus [30]. The materials elastic stiffness coefficients and lattice constants for CuInSe<sub>2</sub>, CuInS<sub>2</sub>, AgGaSe<sub>2</sub>, and AgGaS<sub>2</sub> are presented in Table 1. The correlation trend between overall elastic stiffness N and bulk modulus B for each group, i.e. (CuInS<sub>2</sub>, CuInSe<sub>2</sub>) and (AgGaS<sub>2</sub>, AgGaSe<sub>2</sub>) is clearly shown in Figure 1; the overall elastic stiffness increases as the calculated bulk modulus **B** increases. Besides, the calculated bulk moduli are in good agreement with those found by theory of anisotropy [28] and experimental values [13]. Also, the bulk modulus for each group is inversely proportional to lattice constants a, as shown in Figure 2, which was confirmed in several studies [14-15, 31-32]. Consequently, the overall elastic stiffness N is inversely proportional to lattice constants a, as shown



in figure 3.  $CuInS_2$  and  $AgGaS_2$  have larger elastic stiffness, largest bulk modulus, and lower lattice constant than those for  $CuInSe_2$  and  $AgGaSe_2$ , respectively. Therefore, the overall elastic stiffness and bulk modulus, the only elastic moduli possessed by all states of matter, reveal much about interatomic bonding strength. The bulk modulus also is the most often cited elastic constant to compare interatomic bonding strength among various materials [33], and thereafter the overall elastic stiffness can be cited as well [16].

For the isotropic symmetry material, the elastic stiffness tensor is decomposed into two parts [12, 26-28]; meanwhile, the decomposition of the tetragonal symmetry material, from Eq. (1), is consisted of the same two isotropic decomposed parts and other four terms. The Norm Ratio Criteria (NRC) used in this paper is similar to that proposed in [16, 21]. For isotropic materials, the elastic stiffness tensor has two parts, so the norm of the elastic stiffness tensor for isotropic materials is equal to the norm of these two parts, Eq. (3), i.e.,  $N = N_{iso}$ . Hence, the ratio  $\frac{N_{iso}}{N}$  is equal to one for isotropic materials.

For tetragonal symmetry materials, the elastic stiffness tensor has the same two parts that consisting the isotropic symmetry materials and the other four terms, will be designated as the other than isotropic or the anisotropic part. Hence, two ratios are defined as:  $\frac{N_{iso}}{N}$  for the isotropic parts and

 $\frac{N_{aniso}}{N}$  for the anisotropic parts. The norm ratios can also be used to assess the degree of anisotropy of a material property as a whole. The following criteria are implemented [16]: when  $N_{iso}$  is dominating among norms of the decomposed parts, the closer the norm ratio  $\frac{N_{iso}}{N}$  is to one, the more isotropic the material is. When  $N_{iso}$  is not dominating, norm ratio of the other parts,  $\frac{N_{aniso}}{N}$ , can be used as a criterion. But in this case the situation is reversed; the closer the norm ratio  $\frac{N_{aniso}}{N}$  is to one, the more anisotropic the material is.

The norms and norm ratios for the hetrojunction layer compounds CuInSe<sub>2</sub>, CuInS<sub>2</sub>, AgGaSe<sub>2</sub>, and AgGaS<sub>2</sub> are calculated and shown in Figures 4 and 5; as the isotropic ratio  $\frac{N_{iso}}{N}$  increases, the anisotropic ratio  $\frac{N_{aniso}}{N}$  decreases and this confirms the definitions of these two ratios, and the bulk modulus increases at the same time.



Therefore, CuInS<sub>2</sub> is a closer material to isotropy (or less anisotropy), with  $\frac{N_{iso}}{N} = 0.9859$ , and larger bulk modulus  $\boldsymbol{B} = 64.43$  *GPa* than those for CuInSe<sub>2</sub>. Similarly, AgGaS<sub>2</sub> possesses a closer material structure to isotropy and larger bulk modulus  $\boldsymbol{B}$  than those for AgGaSe<sub>2</sub>.

	$C_{11}$	$C_{12}$	$C_{44}$	$C_{13}$	$C_{33}$	$C_{66}$	а
<b>CuInS</b> <sub>2[34]</sub>	83.7	54.4	34.5	54.8	84.5	33.9	0.5532[37]
CuInSe <sub>2[34]</sub>	71.0	45.3	45.5	45.3	63.3	47.4	0.5782[38]
<b>AgGaS</b> <sub>2[35]</sub>	87.9	58.4	24.1	59.2	84.5	30.8	0.5759[39]
AgGaSe <sub>2[36]</sub>	89.8	65.7	21.7	45.1	63.3	13.3	0.5993[39]

**Table 1** Elastic coefficients (GPa) and lattice constants a (nm) forthe hetrojunction layers compounds



Figure 1 The relation between the overall elastic constant N and bulk modulus B for the hetrujction layer compounds.





Figure 2 The relation between the bulk modulus B and lattice constant a for the hetrujction layer compounds.



Figure 3 The relation between the overall elastic constant N and lattice constant a for the hetrujction layer compounds.





Figure 4 The relation between the overall elastic constant N and isotropy ratio  $\frac{N_{iso}}{N}$  for the hetrujction layer compounds.



Figure 5 The relation between the overall elastic constant N and anisotropy ratio  $\frac{N_{aniso}}{N}$  for the hetrujction layer compounds.



# 4. CONCLUSIONS

A significant contribution of this decomposition method is the direct correlation between the macroscopic and microscopic features of a material by means of symmetry properties. Based on the Orthonormal Tensor Basis Method (OTBM), the elastic stiffness for tetragonal system materials into two parts; isotropic (two terms) and anisotropic (four parts) is presented. The overall elastic stiffness is calculated and correlated with lattice constants and calculated bulk modulus for the hetrojunction layer compounds CuInSe<sub>2</sub>, CuInS<sub>2</sub>, AgGaSe<sub>2</sub>, and AgGaS<sub>2</sub>. The overall elastic stiffness is quantified and correlated to bulk modulus and inversely proportional to lattice constants. CuInS<sub>2</sub> and AgGaS<sub>2</sub> have larger overall elastic stiffness and bulk modulus and the smaller lattice constant than CuInSe<sub>2</sub> and AgGaSe<sub>2</sub>, respectively. Based on the Norm Ratio Criteria (NRC), the hetrojunction layer compounds CuInS<sub>2</sub> are closer to isotropy (or less anisotropic) than CuInSe<sub>2</sub> and AgGaSe<sub>2</sub>.

## **5. REFERENCES**

- Ramesh, P. P., Hussain, O. M., Uthanna, S., Naidu, P. S., Reddy, P. J., (1999), "Characterization of p-AglnSe<sub>2</sub>/n-Zn<sub>0.35</sub>Cd<sub>0.65</sub>S polycrystalline thin film hetrojunction", Materials Science and Engineering B 49, 27-30.
- Ramesh, P. P., Hussain, O. M., Uthanna, S. S., Naidu, P., Reddy, P. J., (1998), "Photovoltaic performance of p-AgInSe<sub>2</sub>/n-Cds thin film hetrojunction", Materials Letters 34, 217-221.
- Murthy, Y., S., Hussain O. M., Naidu, S. B., Reddy, P. J., (1991), "Characterization of p-AglnSe<sub>2</sub>/n-Zn<sub>0.35</sub>Cd<sub>0.65</sub>S polycrystalline thin film hetrojunction", Materials Letters 10, 504-508.
- 4. Shay, J. L., Wernick, J. H., (1974), Ternary Chalcopyrite Semiconductors: Growth, Electronic Properties and Applications, Pergamon Press, Oxford.
- Choi, In-Hwan, Yu, P. Y., (1996), "Optical investigation of defects in AgGaS<sub>2</sub> and CuGaS<sub>2</sub>", Journal of Chemistry and Physics of Solids 57, 1695-1704.
- Reddy, R. R., Ahmmed Y. N., Gopal, K. R., Abdul Azeem P., Rao, T. V. R., Reddy, P. M., (2000), "Optical Electronegativity, bulk modulus and electronic polarizability of materials", Optical Materials 14, 355-358.
- Chandra, G. H., Hussain, O. M., Uthanna, S., Naidu, B. S., (2002), "Potovoltaic performance of p-Ag Ga<sub>0.25</sub>In<sub>0.75</sub>Se<sub>2</sub>/n-Cds thin film hetrojunctions", Materials Letters 53, 216-220.



- 8. Eom, S. H., Kim, D. J., Yu, Y. M., Chi, Y. D., (2005), "Temperature dependent absorption edge in AgGaS<sub>2</sub> compound semiconductor", Journal of Alloys and Compounds 388, 190-194.
- Chahed, A., Benhelal, O., Laksari S., Abbar, B., Bouhafs, B., Amrane, N., (2005), "First principles calculations of the structural, electronic and optical properties of AgGaS<sub>2</sub> and AgGaSe<sub>2</sub>", Physica B 367, 142-151.
- Mustafa, H., Hunter, D., Pradhan, A. K., Roy, U. N., Cui, Y., Burger, A., (2007), "Synthesis and characterization of AgInSe2 for application in thin film solar cells", Thin Solid Films 515, 7001-7004.
- 11. Roy, U. N., Cui, Y., Hawrami, R., Burger, A., Orona, L., Goldstein, J. T., (2006), "AgGaS2<sub>2</sub>: A highly photoconductive material", Solid State Communications 139, 527-530.
- 12. **Kim E. and Chen C., (2004),** "Calculation of bulk modulus for highly anisotropic materials", Physics Letters A 326, 442-448.
- 13. Cohen M. L., (1985), "Calculation of bulk moduli of diamond and zinc-blende solids", Physical Review B 32, 7988-7991.
- 14. Lam, P. K., Cohen, M. L., Martinez, G., (1987), "Analytic relation between bulk moduli and lattice constants", Physical Review B 35, 9190.
- Al-Douri, Y, Abid, H., Aourag, H., (2004), "Empirical formula relating the bulk modulus to the lattice constant in tetrahedral semiconductors", Materials Chemistry and Physics 87, 14-17.
- Gaith, M., Alhayek, I., (2009), "Correlation Between Overall Elastic Stiffness, Bulk Modulus and Interatomic Distance in Anisotropic Materials: Semiconductors", Review of Advance Material Sciences 21, 183-191.
- 17. Gaith, M., Alhayek, I., (2009), "The Calculation of Stiffness for Semiconductor Components", Proceedings of the ASME 2009 on Smart Materials, Adaptive Structures and Intelligent Systems, SMASIS2009, September 20-24, 2009, Oxnard, California, USA.
- Gaith, M., Alhayek, I., (2009), "The Measurement of Overall Elastic Stiffness and Bulk Modulus in Anisotropic Materials: Semiconductors", Proceedings of the ASME 2009 International Mechanical Engineering Congress & Exposition IMECE 2009 November 13-19, 2009, Lake Buena Vista, Florida, USA.
- Tu., Y.O., (1968), "The Decomposition of anisotropic elastic tensor", Acta Crystallographica A 24, 273-282.
- 20. Jerphagnon, J., Chemla, D.S., Bonnevile, R., (1978), "The decomposition of condensed matter using irreducible tensors", Advances in Physics 27, 609-650.



- Gaith, M., Akgoz, C.Y., (2005), "A new representation for the properties of anisotropic elastic fiber reinforced composite materials", Review of Advance Material Sciences 10, 138-142.
- 22. Srinivasan, T. P., Nigam, S. D., (1968), "Invariant forms", Journal of Math. Phys. Sci. 2, 311-320.
- 23. Srinivasan, T. P., (1970), "Invariant piezoelectric coefficients for crystals", Physica Status Solidi B 41, 615-620.
- 24. Srinivasan, T. P., (1969), "Invariant elastic constants for crystals", Journal of Mathematics and Mechanics 19, 411-420.
- 25. Srinivasan, T. P., (1985), "Invariant acoustic gyrotropic coefficients", Journal of Physics C 18, 3263-3271.
- 26. Spencer, A. T. M., (1983), Continuum Mechanics, Longmans: London.
- 27. Voigt, W., (1889), "The relation between the two elastic moduli of isotropic materials", Annals of Physics, (Leipzig) 33, 573.
- 28. **Hearmon, R., (1961),** An Introduction to Applied Anisotropic Elasticity, Oxford University Press.
- Fischer, C.H., Batzer, M., Glatzel, T., Lauermann, I., M.C. Lux-Steiner, M.C., (2006), "Interface engineering in chalcopyrite thin film solar devices", Solar Energy Materials & Solar Cells 90, 1471-1585.
- Bätzner, D. L., Romeo, A., Terheggen, M., Döbeli, M., Zogg, H., Tiwari, A. N., (2004), "Stability aspects in CdTe/CdS solar cells", Thin Solid Films 451, 536-543.
- 31. Christensen, N. E., Christensen, O. B., (1986), "Electronic structure of ZnTe and CdTe under pressure", Physical Review B 33, 4739-4746.
- 32. Al-Douri, Y., Abid, H., Aourag, H., (2001), "Correlation between the bulk modulus and the charge density in semiconductors", Physica B 305, 186-190.
- 33. Pantea, C., Mihut, I., Ledbetter, H., Betts, J.B., Zhao, Y., Daemen, L.L., Cynn, H., Miglori, A., (2009), "Bulk modulus of osmium", Acta Materialia 57, 544-548.
- 34. Lażewski, J., Neumann, H., Jochym, P. T., Parlinski, K., (2003), "Ab initio elasticity of chalcopyrites", Journal of Applied Physics 93, 3789-37896.
- Grimsditch, N. S., Holah, G. D., (1975), "Brillouin scattering and elastic moduli of silver thiogallate (AgGaS<sub>2</sub>)", Physical Review B 12, 4377-4382.



- Eimerl, D., Marion, J., Graham, E. K., McKinstry, H. A., Haussuhl, S., (1991), "Elastic constants and thermal fracture of AgGaSe<sub>2</sub> and d-Lap", IEEE Journal of Quantum Electrnics 27, 142-145.
- 37. Krustok, J., Raudija, J., Collan, H., (2001), "Photoluminescence and the tetragonal distortion in CuInS<sub>2</sub>", Thin Solid Films 387, 195-197.
- 38. Kannan, M.D., Balasundaraprabhu, R., Jayakumar, S., Ramanathaswamy, P., (2004), "preparation and study of structural and optical properties of CSVT deposited CuInSe<sub>2</sub> thin films", Solar Energy Materials & Solar Cells 81, 379-395.
- 39. Chahed, A., Benhelal, O., Laksari, S., Abbar, B., Bouhafs, B., Amrane, N., (2005), "Firstprinciples calculations of the structural, electronic and optical properties of AgGaS<sub>2</sub> and AgGaSe<sub>2</sub>". Physica B 367, 142-151.